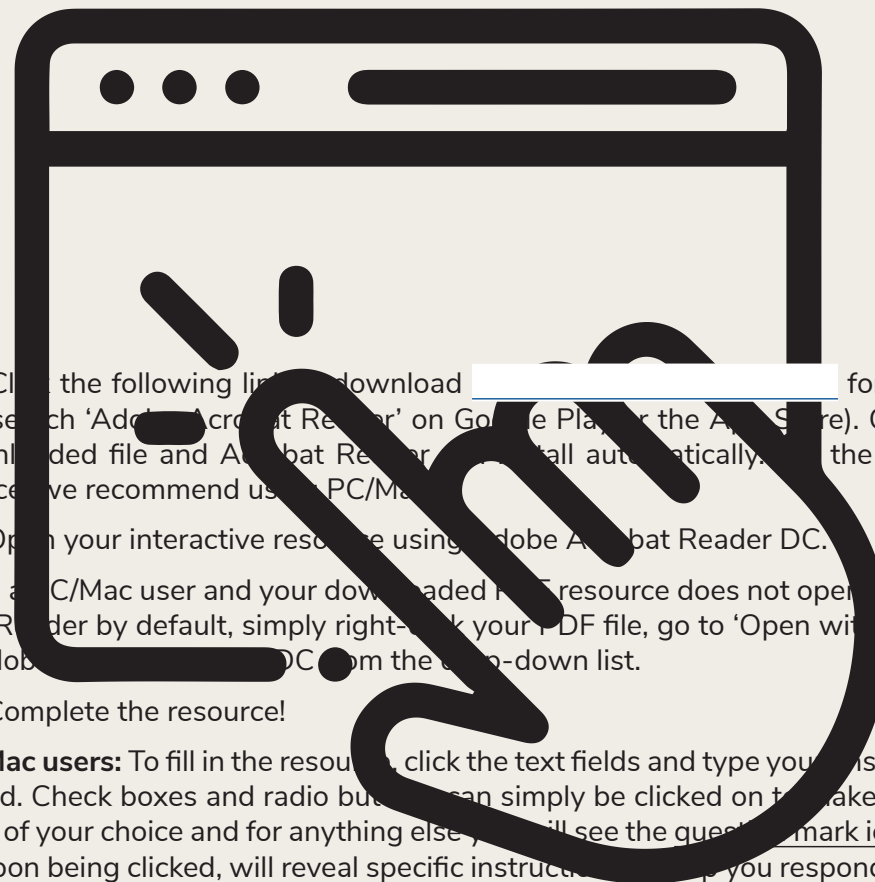




## Thanks for downloading this resource!

The zip folder that you've just opened contains a PDF file with **interactive features**.

In a move towards offering an even more versatile spread of resources, some of our worksheets feature interactive fields that can be filled in on computers and smart devices, without having to print the page. Follow the guidance in the next column for a smooth, stress-free means of accessing this content using free-to-download PDF reading software.



**Step 1:** Click the following link to download [Adobe Acrobat Reader DC](#) for PC/Mac (or search 'Adobe Acrobat Reader' on Google Play or the App Store). Open the downloaded file and Adobe Acrobat Reader will install automatically. For the best experience we recommend using PC/Mac.

**Step 2:** Open your interactive resource using Adobe Acrobat Reader DC.

If you are a PC/Mac user and your downloaded PDF resource does not open using Acrobat Reader by default, simply right-click your PDF file, go to 'Open with' and select Adobe Acrobat Reader DC from the drop-down list.

**Step 3:** Complete the resource!

**For PC/Mac users:** To fill in the resource, click the text fields and type your answers as needed. Check boxes and radio buttons can simply be clicked on to make the selection of your choice and for anything else you will see the question mark icon which, upon being clicked, will reveal specific instructions for you respond to the corresponding question or activity. When you are finished with the resource, go to File > Save As... and save your file in a memorable location.

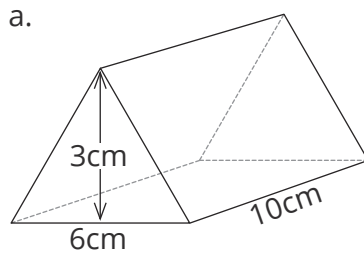
**For smart device users:** To fill in the resource, follow the same process as described above. When you are finished, simply press the back button in the top left of the appscreen and your PDF will save automatically.

**Remember:** Saving your PDF will overwrite the original file, so be sure to create a copy before starting if you wish to keep a blank copy of the resource on your device.

We hope you have found this information useful. If you experience any problems in following the instructions above, please contact the Beyond team at [beyond@regentstudies.com](#) and we will do our best to help with your query.

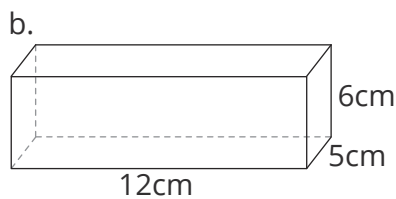
## Your turn

1. Calculate the volume of each shape, giving your answers correct to the nearest whole number where necessary.

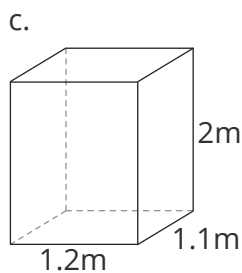


$$\frac{1}{2} \times 6 \times 3 = 9\text{cm}^2$$

$$9 \times 10 = 90\text{cm}^3$$

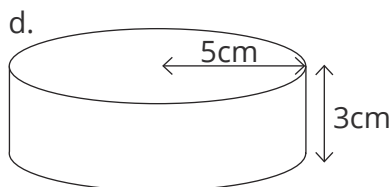


$$5 \times 6 \times 12 = 360\text{cm}^3$$



$$2 \times 1.1 \times 1.2 = 2.64$$

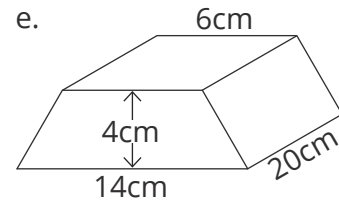
$$3\text{m}^3$$



$$\pi \times 5^2 = 78.53981634...\text{cm}^2$$

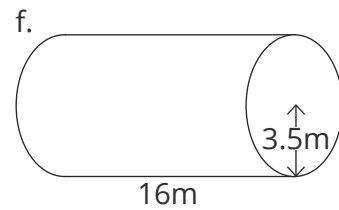
$$78.53981634... \times 3 = 235.619449...\text{cm}^2$$

$$236\text{cm}^3$$



$$\frac{1}{2} \times (6 + 14) \times 4 = 40\text{cm}^2$$

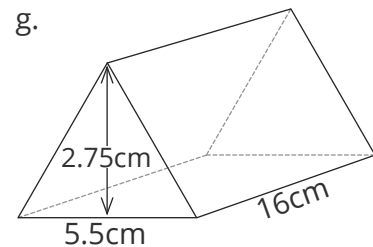
$$40 \times 20 = 800\text{cm}^3$$



$$\pi \times 3.5^2 = 38.48451001...\text{m}^2$$

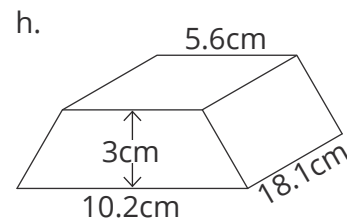
$$38.48451001... \times 16 = 615.7521601...$$

$$616\text{m}^3$$



$$\frac{1}{2} \times 5.5 \times 2.75 = 7.5625\text{cm}^2$$

$$7.5625 \times 16 = 121\text{cm}^3$$

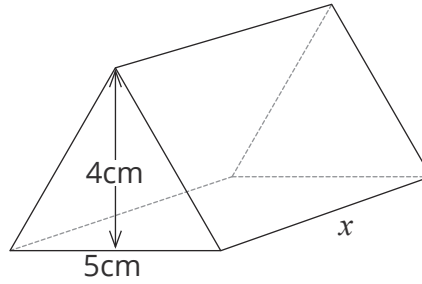


$$\frac{1}{2} \times (5.6 + 10.2) \times 3 = 23.7\text{cm}^2$$

$$23.7 \times 18.1 = 428.97$$

$$429\text{cm}^3$$

2. The volume of the triangular prism is  $106\text{cm}^3$ . Calculate the measurement of the missing length marked  $x$ .

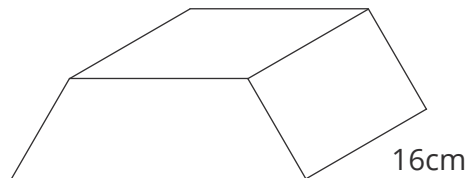


$$\frac{1}{2} \times 4 \times 5 = 10\text{cm}^2$$

$$106 \div 10 = 10.6$$

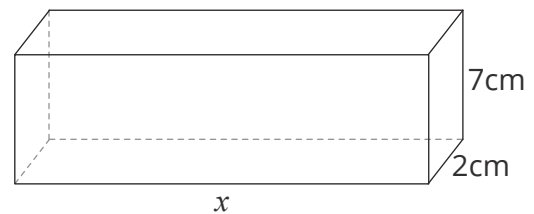
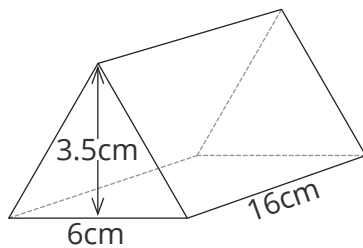
$$x = 10.6\text{cm}$$

3. The volume of the prism shown below is  $216\text{cm}^3$ . Calculate the cross-sectional area of the prism.



$$216 \div 16 = 13.5\text{cm}^2$$

4. The cuboid and the triangular prism have the same volume. Calculate the measurement of the missing length marked  $x$ .



$$\frac{1}{2} \times 6 \times 3.5 = 10.5\text{cm}^2$$

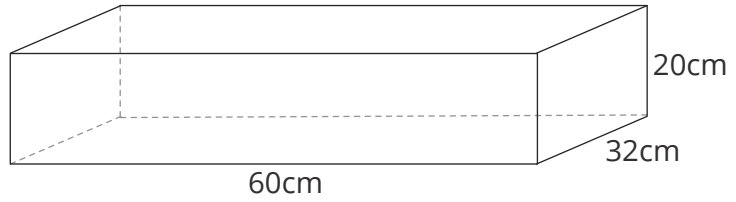
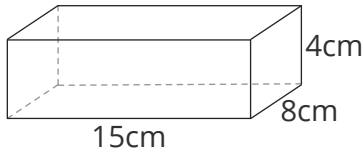
$$10.5 \times 16 = 168\text{cm}^3$$

$$7 \times 2 = 14\text{cm}^2$$

$$168 \div 14 = 12$$

$$x = 12\text{cm}$$

5. Boxes of chocolate are placed into a crate. Each box of chocolate is a cuboid and the crate is also a cuboid. Calculate the number of boxes of chocolate which will fit inside the crate.



$$60 \div 15 = 4\text{cm}$$

$$32 \div 8 = 4\text{cm}$$

$$20 \div 4 = 5\text{cm}$$

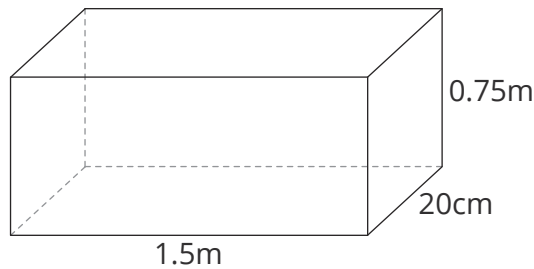
$$4 \times 4 \times 5 = 80$$

**80 boxes of chocolate will fit inside of the crate.**

### Challenge

A fish tank is filled  $\frac{3}{4}$  full of water. Joshua pours 1500ml more water into the fish tank. How many **litres** of water does the fish tank now contain?

Hint:  $1\text{ml} = 1\text{cm}^3$



$$1.5\text{m} = 150\text{cm}$$

$$0.75\text{m} = 75\text{cm}$$

$$150 \times 20 \times 75 = 225\,000\text{cm}^3$$

$$225\,000\text{cm}^3 = 225\,000\text{ml}$$

$$\frac{3}{4} \times 225\,000 = 168\,750\text{ml}$$

$$168\,750 + 1500 = 170\,250\text{ml}$$

$$170\,250\text{ml} = 170.25\text{ litres}$$

# Volume of Prisms

## Prior Knowledge:

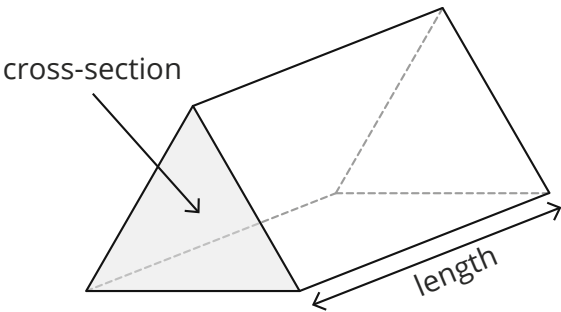
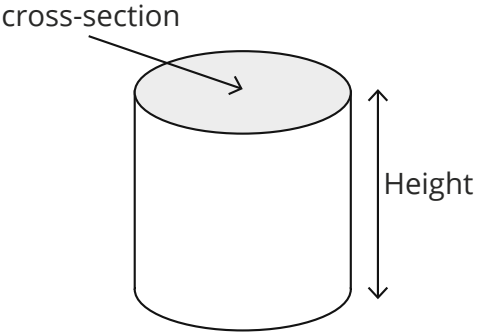
Before attempting this sheet, students should be able to:

- calculate the area of a circle ( $\pi r^2$ )
- round numbers to whole numbers
- calculate the area of:
  - triangles ( $\frac{1}{2} \times \text{base} \times \text{height}$ )
  - rectangles (length  $\times$  width)
  - squares (length  $\times$  width)
  - trapeziums ( $\frac{1}{2} \times (a + b) \times \text{height}$ )

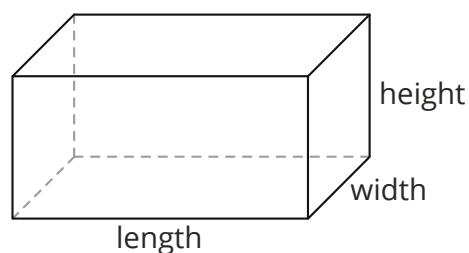
The volume of a shape is the measure of the **three-dimensional** space it covers. The units of measurement for volume are cubic units, for example  $\text{cm}^3$  or  $\text{m}^3$ .

A **prism** is a solid (3D) object which is the same shape all the way through; it has a constant cross-section.

To calculate the volume of a prism, including a circular prism, learn this formula by heart:

Volume = area of cross-section $\times$ length or height	
	

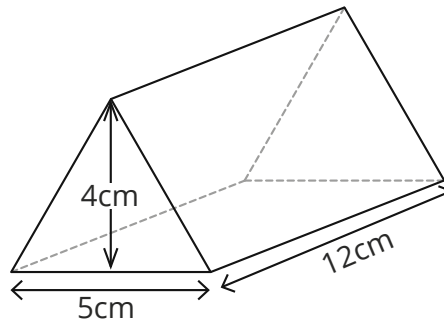
For example, the cross-section of this cuboid is a rectangle.



To calculate the area of the cross-section, it would be length  $\times$  width. You would then multiply this by the height, hence the formula: length  $\times$  width  $\times$  height.

**Example 1**

Calculate the volume of the prism shown below.



The first step is to calculate the **area of the cross-section**. In other words, you need to calculate the area of the **base** of the shape. (The **base** is always the face which is the same as the cross-section).

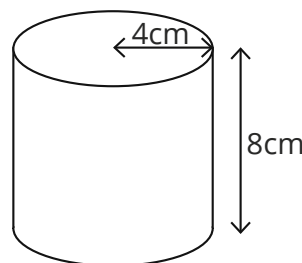
This shape is a triangular prism; its base is a triangle. Therefore, you need to calculate the area of the triangle. Remember that the formula for calculating the area of a triangle is  $\frac{1}{2} \times \text{base} \times \text{height}$ .

$$\frac{1}{2} \times 5 \times 4 = 10\text{cm}^2$$

Now that you have the area of the cross-section, multiply it by its length to calculate the volume.  
 $10 \times 12 = 120\text{cm}^3$  (Don't forget the units!)

**Example 2**

Calculate the volume of the cylinder, giving your answer correct to the nearest whole number.



Start by calculating the area of the cross section. In other words - the area of the circle. Remember that the formula for calculating the area of a circle is  $\pi r^2$ .

$$\pi \times 4^2$$

$$\pi \times 16 = 50.26548246\dots\text{cm}^2$$

(It's important that you don't round your answer at this stage – you could also leave your answer in terms of  $\pi$ , e.g.  $16\pi$ .)

Now, multiply the area of the circle by the height.

$$50.26548246\dots \times 8 = 402.1238597\dots$$

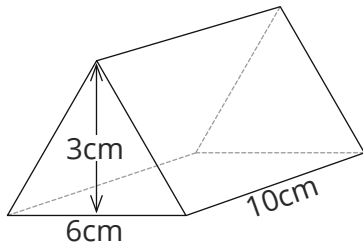
As you don't have any further calculations to do, you should now round the answer to the degree which the question has asked for. In this case, the nearest **whole** number.

Therefore, the answer is **402cm<sup>3</sup>**. (Don't forget the units!)

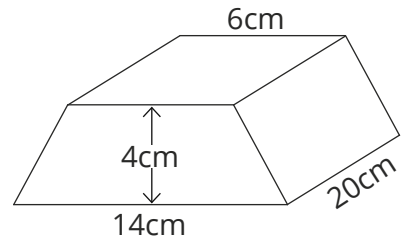
**Your turn**

1. Calculate the volume of each shape, giving your answers correct to the nearest whole number where necessary.

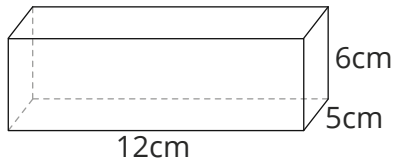
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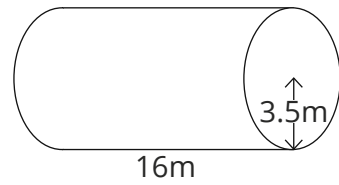
e.



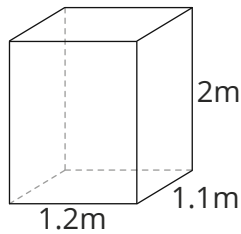
b.



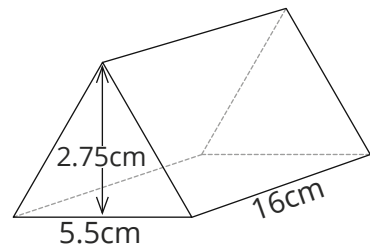
f.



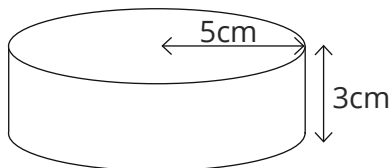
c.



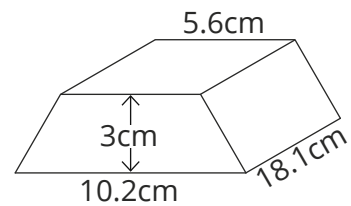
g.



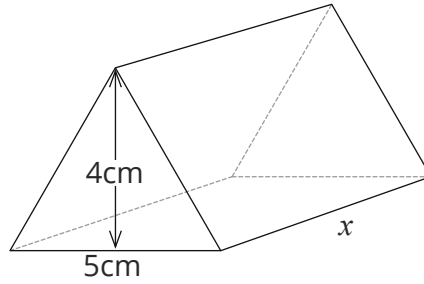
d.



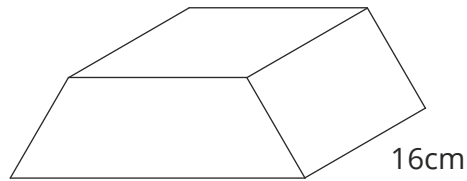
h.



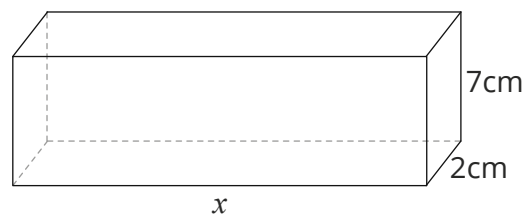
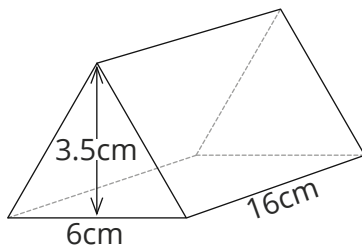
2. The volume of the triangular prism is  $106\text{cm}^3$ . Calculate the measurement of the missing length marked  $x$ .



3. The volume of the prism shown below is  $216\text{cm}^3$ . Calculate the cross-sectional area of the prism.

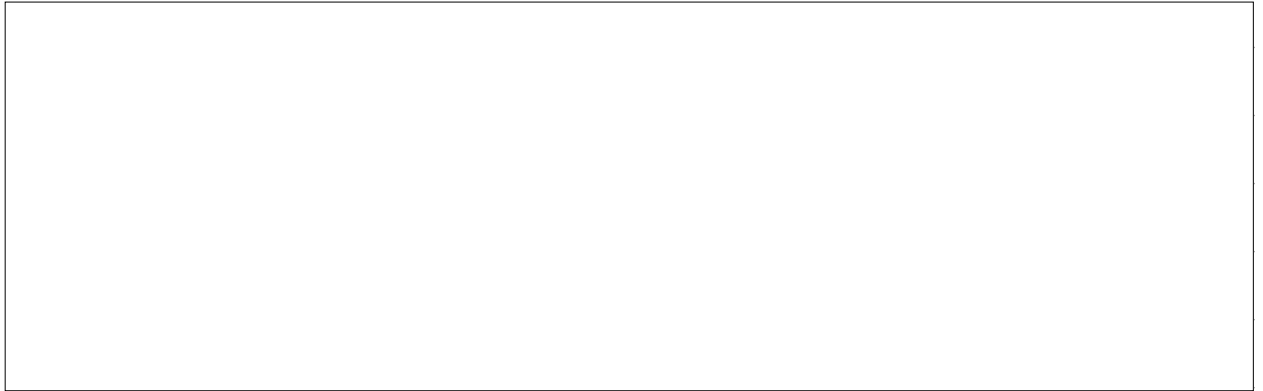
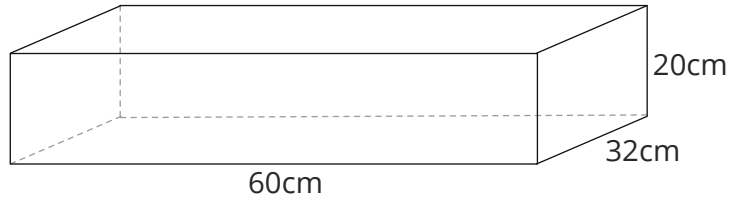
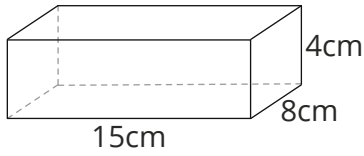


4. The cuboid and the triangular prism have the same volume. Calculate the measurement of the missing length marked  $x$ .





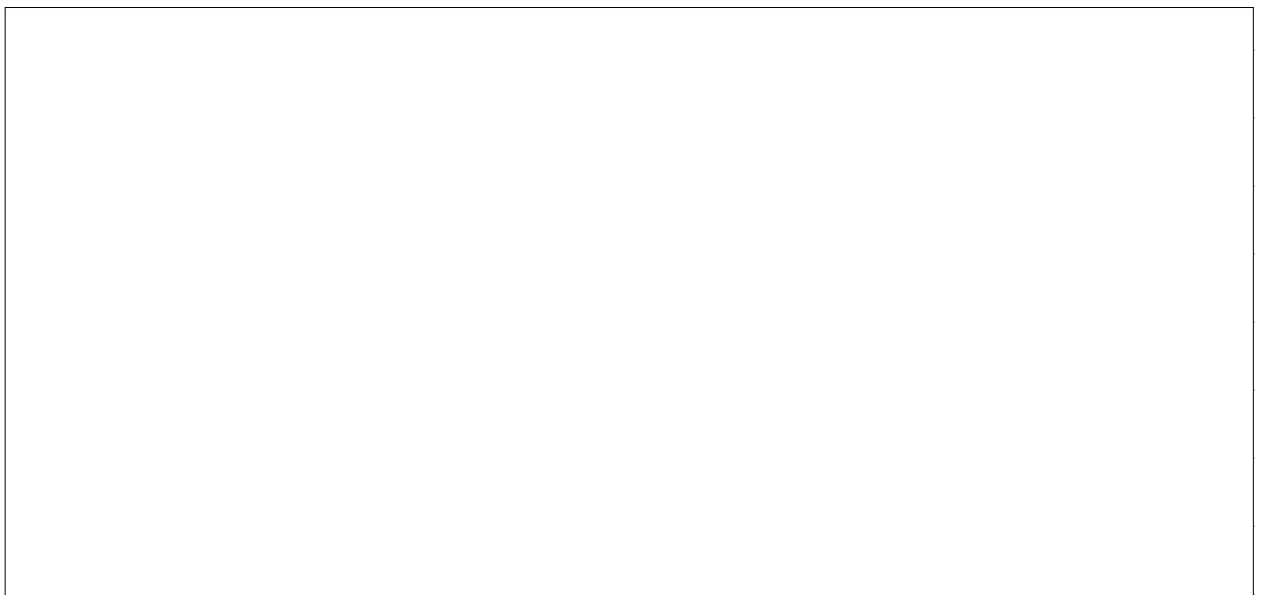
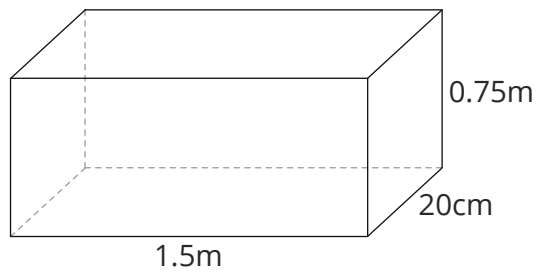
5. Boxes of chocolate are placed into a crate. Each box of chocolate is a cuboid and the crate is also a cuboid. Calculate the number of boxes of chocolate which will fit inside the crate.



**Challenge**

A fish tank is filled  $\frac{3}{4}$  full of water. Joshua pours 1500ml more water into the fish tank. How many **litres** of water does the fish tank now contain?

Hint: 1ml = 1cm<sup>3</sup>



# Volume of Prisms

## Prior Knowledge:

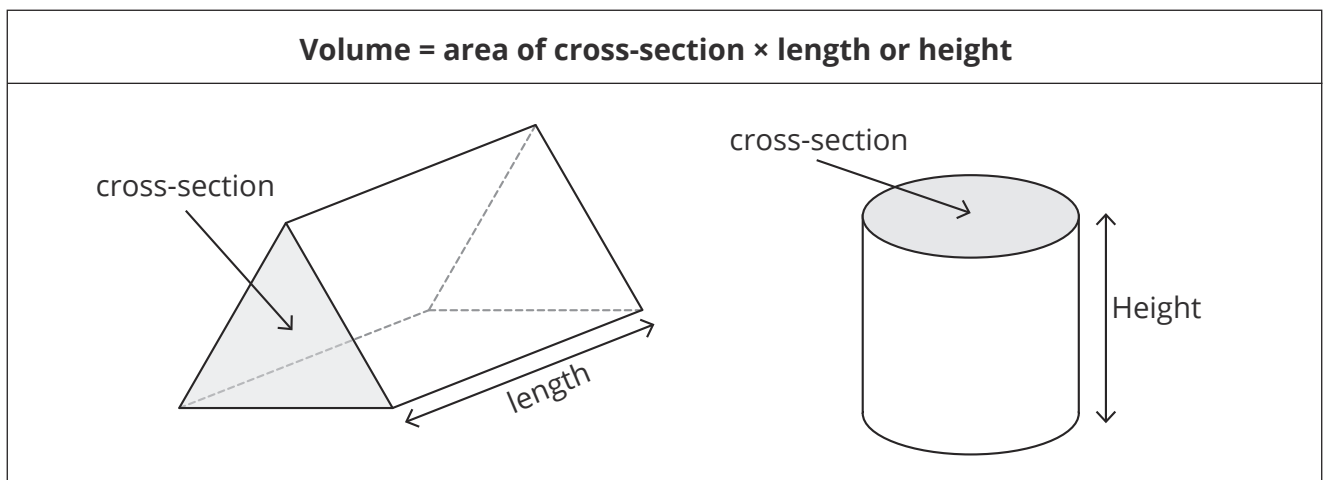
Before attempting this sheet, students should be able to:

- calculate the area of a circle ( $\pi r^2$ )
- round numbers to whole numbers
- calculate the area of:
  - triangles ( $\frac{1}{2} \times \text{base} \times \text{height}$ )
  - rectangles (length  $\times$  width)
  - squares (length  $\times$  width)
  - trapeziums ( $\frac{1}{2} \times (a + b) \times \text{height}$ )

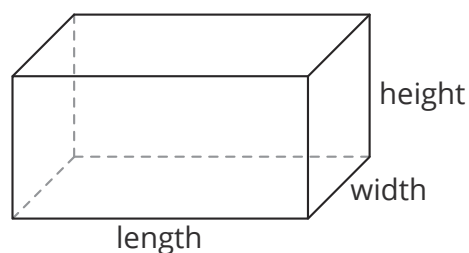
The volume of a shape is the measure of the **three-dimensional** space it covers. The units of measurement for volume are cubic units, for example  $\text{cm}^3$  or  $\text{m}^3$ .

A **prism** is a solid (3D) object which is the same shape all the way through; it has a constant cross-section.

To calculate the volume of a prism, including a circular prism, learn this formula by heart:



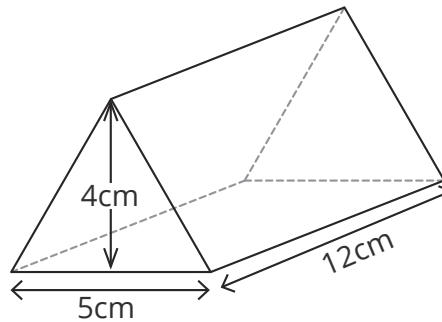
For example, the cross-section of this cuboid is a rectangle.



To calculate the area of the cross-section, it would be length  $\times$  width. You would then multiply this by the height, hence the formula: length  $\times$  width  $\times$  height.

**Example 1**

Calculate the volume of the prism shown below.



The first step is to calculate the **area of the cross-section**. In other words, you need to calculate the area of the **base** of the shape. (The **base** is always the face which is the same as the cross-section).

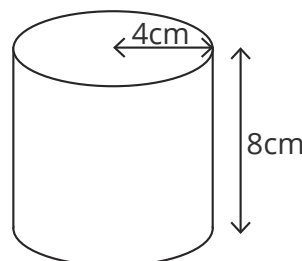
This shape is a triangular prism; its base is a triangle. Therefore, you need to calculate the area of the triangle. Remember that the formula for calculating the area of a triangle is  $\frac{1}{2} \times \text{base} \times \text{height}$ .

$$\frac{1}{2} \times 5 \times 4 = 10\text{cm}^2$$

Now that you have the area of the cross-section, multiply it by its length to calculate the volume.  
 $10 \times 12 = 120\text{cm}^3$  (Don't forget the units!)

**Example 2**

Calculate the volume of the cylinder, giving your answer correct to the nearest whole number.



Start by calculating the area of the cross section. In other words - the area of the circle. Remember that the formula for calculating the area of a circle is  $\pi r^2$ .

$$\pi \times 4^2$$

$$\pi \times 16 = 50.26548246\dots\text{cm}^2$$

(It's important that you don't round your answer at this stage – you could also leave your answer in terms of  $\pi$ , e.g.  $16\pi$ .)

Now, multiply the area of the circle by the height.

$$50.26548246\dots \times 8 = 402.1238597\dots$$

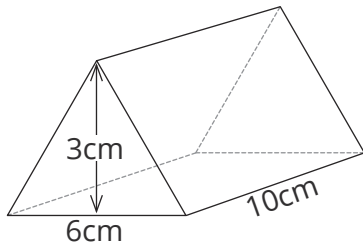
As you don't have any further calculations to do, you should now round the answer to the degree which the question has asked for. In this case, the nearest **whole** number.

Therefore, the answer is **402cm<sup>3</sup>**. (Don't forget the units!)

**Your turn**

1. Calculate the volume of each shape, giving your answers correct to the nearest whole number where necessary.

a.




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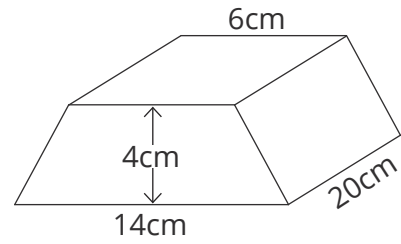


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e.




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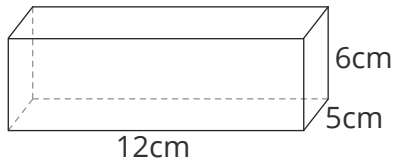


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b.




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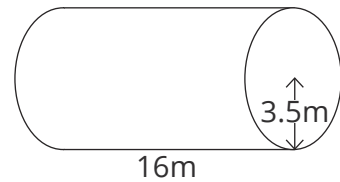


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f.




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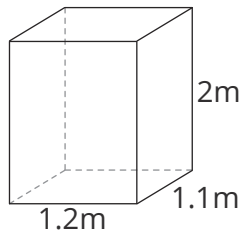


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c.




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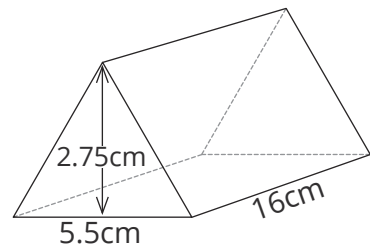


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g.




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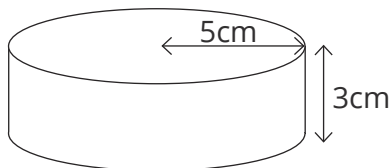


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d.




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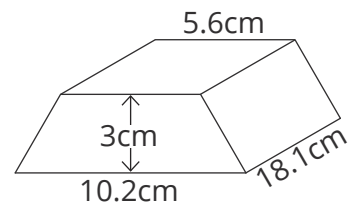


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h.




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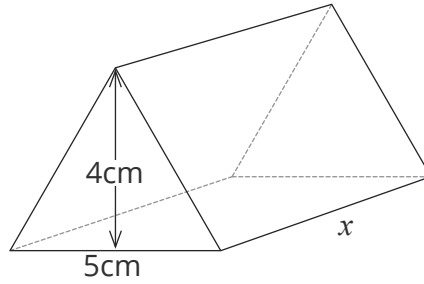


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2. The volume of the triangular prism is  $106\text{cm}^3$ . Calculate the measurement of the missing length marked  $x$ .




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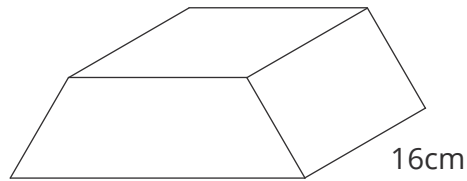


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3. The volume of the prism shown below is  $216\text{cm}^3$ . Calculate the cross-sectional area of the prism.




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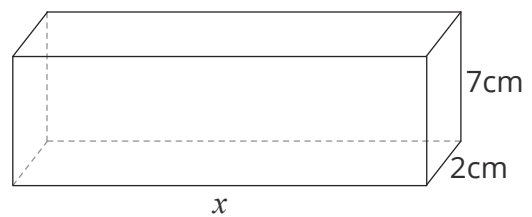
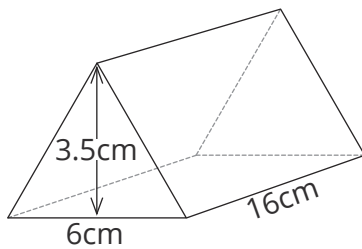


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4. The cuboid and the triangular prism have the same volume. Calculate the measurement of the missing length marked  $x$ .




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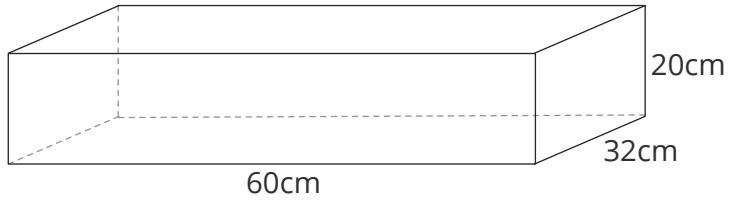
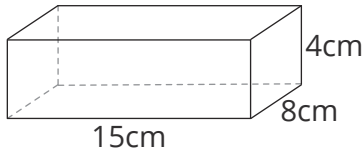


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5. Boxes of chocolate are placed into a crate. Each box of chocolate is a cuboid and the crate is also a cuboid. Calculate the number of boxes of chocolate which will fit inside the crate.



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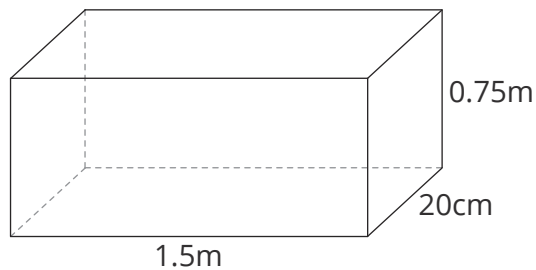
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**Challenge**

A fish tank is filled  $\frac{3}{4}$  full of water. Joshua pours 1500ml more water into the fish tank. How many **litres** of water does the fish tank now contain?

Hint: 1ml = 1cm<sup>3</sup>



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